Data on the Heap

num bool × Char × double

Next, lets add support for

Data Structures

In the process of doing so, we will learn about

- Heap Allocation
- Run-time Tags

· High-order Func (Closures)

Lenv, code)

Creating Heap Data Structures

We have already support for two primitive data types

data Ty
 = TNumber -- e.g. 0,1,2,3,...
 | TBoolean -- e.g. true, false

we could add several more of course, e.g.

- Char
- Double or Float

etc. (you should do it!)

However, for all of those, the same principle applies, more or less

• As long as the data fits into a single word (8-bytes)

Instead, lets learn how to make unbounded data structures

- Lists
- Trees
- ...

which require us to put data on the **heap**

not just the stack that we've used so far.





Stack vs. Heap

Pairs

While our goal is to get to lists and trees, the journey of a thousand miles begins with

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(9, 12)



Pairs: Semantics (Behavior)

First, lets ponder what exactly we're trying to achieve.

We want to enrich our language with two new constructs:

- **Constructing** pairs, with a new expression of the form (e0, e1) where e0 and e1 are expressions.
- Accessing pairs, with new expressions of the form e[0] and e[1] which

1

evaluate to the first and second element of the tuple e respectively.

For example,

let t = (2, 3) in
 t[0] + t[1]

should evaluate to 5.

Strategy

Next, lets informally develop a strategy for extending our language with pairs, implementing the above semantics. We need to work out strategies for:

1. Representing pairs in the machine's memory,

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asm>

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https://ucsd-cse131.github.io/sp21/lectures/07-egg-eater.html

(asm)

2. **Constructing** pairs (i.e. implementing (e0, e1) in assembly),

3. Accessing pairs (i.e. implementing e[0] and e[1] in assembly).

1. Representation

Recall that we represent all values: (05-cobra.md/#option-2-use-a-tag-bit)

64

- Number like 0, 1, 2 ...Boolean like true, false

as a single word either

- 8 bytes on the stack, or
- a single register rax, rbx etc.

EXERCISE

What kinds of problems do you think might arise if we represent a pair (2, 3) on the *stack* as:



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def tail(le): lF17 Eloj (1,2) 3 (1,2) 3 (1,2) (2,2)def is Nil (U): L== False def nills: false def cons(h,t): (h,t) (def range (lo, hi): if lochi: Cons(lo, raye(lo+1, hi)) dse: How many words would we need to store the tuple build 5 (3, (4, 5))vil () 1. 1 word def length(l): If isNille): 2. 2 words 3. 3 words 4. 4 words 5. 5 words else: l = (a nye(0, 100)) l = (l + length(l))tup 5/13/21, 9:19 AM





Pointers

Every problem in computing can be solved by adding a level of indirection.

We will **represent a pair** by a **pointer** to a block of **two adjacent words** of memory.



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Pairs on the heap

The above shows how the pair (2, (3, (4, 5))) and its sub-pairs can be stored in the **heap** using pointers.

- (4, 5) is stored by adjacent words storing
 - 4 and
 - 5
- (3, (4, 5)) is stored by adjacent words storing
 - 3 and
 - a **pointer** to a heap location storing (4, 5)
- (2, (3, (4, 5))) is stored by adjacent words storing
 - 2 and
 - a **pointer** to a heap location storing (3, (4, 5)).

A Problem: Numbers vs. Pointers?

How will we tell the difference between numbers and pointers?

That is, how can we tell the difference between

- 1. the number 5 and
- 2. a pointer to a block of memory (with address 5)?

Each of the above corresponds to a different tuple

1. (4, 5) or

2. (4, (...)).

so its pretty crucial that we have a way of knowing which value it is.

t = (1, (2, 3))

Tagging Pointers

As you might have guessed, we can extend our tagging mechanism (05cobra.md/#option-2-use-a-tag-bit) to account for *pointers*.



(We have 3-bits worth for tags, so have wiggle room for other primitive types.)

Address Alignment

As we have a 3 bit tag

leaving 64 - 3 = 61 bits for the actual address

So actual addresses, written in binary, omitting trailing zeros, are of the form

Binary	Decimal
0b00000 <mark>000</mark>	0
0b00001 <mark>000</mark>	8
0b00010 <mark>000</mark>	16
0b00011 <mark>000</mark>	<mark>24</mark>
0b00100 <mark>000</mark>	32

That is, the addresses are 8-byte aligned.

Which is great because at each address, we have a pair, i.e. a **2-word = 16-byte block**, so the *next* allocated address will *also* fall on an 8-byte boundary.



• But ... what if we had 3-tuples? or 5-tuples? ...



Next, lets look at how to implement pair **construction** that is, generate the assembly for expressions like:

(e1, e2)

To **construct** a pair (e1, e2) we

1. Allocate a new 2-word block, and getting the starting address at rax,

2. Copy the value of e1 (resp. e2) into [rax] (resp. [rax + 8]).

3. Tag the last bit of rax with 1.

The resulting eax is the value of the pair

• The *last step* ensures that the value carries the proper tag.

ANF will ensure that e1 and e2 are immediate expressions (04-boa.md/#ideaimmediate-expressions)

• will make the second step above straightforward.

EXERCISE How will we do ANF conversion for (e1, e2)?

Allocating Addresses

Lets use a **global** register r15 to maintain the address of the **next free block** on the heap.

Every time we need a *new* block, we will:

- 1. Copy the current r15 into rax
 - Set the last bit to 1 to ensure proper tagging.
 - rax will be used to fill in the values
- 2. Increment the value of r15 by 16

• Thus allocating 8 bytes (= 2 words) at the address in rax

Note that addresses stay 8-byte aligned (last 3 bits = 0) if we

- Start our blocks at an 8-byte boundary, and
- Allocate 16 bytes at a time,

NOTE: Your assignment will have blocks of varying sizes

• You will have to maintain the 8-byte alignment by padding

Example: Allocation

In the figure below, we have

- a source program on the left,
- the ANF equivalent next to it.







Example of Pairs

The figure below shows the how the heap and r15 evolve at points 1, 2 and 3:



Allocating Pairs on the Heap

QUIZ

In the ANF version, p is the *second* (*local*) *variable* stored in the stack frame. What *value* gets moved into the *second stack slot* when evaluating the above program?

1.
$$0 \times 3$$
 ? ?
2. $(3, (4, 5))$?
3. 0×11 $1 \to 17$
4. 0×9 ? ?
5. 0×10 16 16
 $e[0]$ $f \times e(e)$
 $f \times e(bx+8:i)$
 $e[1]$ $f \times e(bx+8:i)$

3. Accessing

Finally, to access the elements of a pair

Lets compile e[0] to get the first or e[1] to get the second element

- 1. Check that immediate value e is a pointer
- 2. Load e into rbx
- 3. Remove the tag bit from rbx

4. Copy the value in [rbx] (resp. [rbx + 8]) into rbx.



4

5

3

Here is a snapshot of the heap after the pair(s) are allocated.



y	Ox8	1
ang	Ox1	
X	Ox6	
P	0×11	
anto	OXL	



Allocating Pairs on the Heap

Lets work out how the values corresponding to x, y and z in the example above get stored on the stack frame in the course of evaluation.

Variable	Hex Value	Value
anf0	0×001	ptr 0
р	0x011	ptr 16
x	0x006	num 3
anf1	0x001	ptr 0
У	0×008	num 4
z	0x00A	num 5
anf2	0x00E	num 7
result	0x018	num 12

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(1, (2, (3, 4)))

Plan

Pretty pictures are well and good, time to build stuff!



We've already built up intuition of the *strategy* for implementing tuples. Next, lets look at how to implement each of the above.

Run-Time

We need to extend the run-time (c-bits/main.c) in two ways.

1. Allocate a chunk of space on the heap and pass in start address to our_code.

2. **Print** pairs properly.

Allocation

The first step is quite easy we can use calloc as follows:

1. Allocates a big block of contiguous memory (starting at HEAP), and

2. Passes this address in to our_code.

Now, our_code needs to, at the beginning start with instructions that

- copy the parameter (in rdi) into global pointer (r15)
- and then bump it up at each allocation.

> alloc >> print

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 $\frac{\langle k+l \rangle \vee_{0} \vee_{1} \vee_{2} \cdots \vee_{k}}{p_{i} = 001}$ To print pairs, we must recursively traverse pointers

• until we hit number or boolean.

We can check if a value is a pair by looking at its last 3 bits:

```
int isPair(int p) {
    return (p & 0x00000007) == 0x00000001;
}
```

We can use the above test to recursively print (word)-values:

```
void print(long val) {
 if(val & 0x1 == 0) { // val is a number
   printf("%ld", val >> 1);
  }
  else if(val == CONST TRUE) { // val is true
   printf("true");
  }
 else if(val == CONST_FALSE) { // val is false
   printf("false");
  }
  else if(val & 7 == 1) {
    long* valp = (long *) (val - 1); // extract address
   printf("(");
   print(*valp);
                                     // print first element
   printf(", ");
   print(*(valp + 1));
                                     // print second element
   printf(")");
  }
 else {
   printf("Unknown value: %#010x", val);
  }
```

}

e, [ez]

Types

Next, lets move into our compiler, and see how the core types need to be extended.

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NOTE: Your assignment will generalize pairs to n-ary tuples using

- Tuple [Expr a] representing (e1,...,en)
- GetItem (Expr a) (Expr a) representing e1[e2]

Dynamic Types

Let us extend our **dynamic types** Ty see (05-cobra.md/#types) to include pairs:

Assembly

The assembly Instruction are changed minimally; we just need access to r15 which will hold the value of the *next* available memory block:

data Register



Transforms

Our code must take care of three things:



The latter two will be pointed out as cases in anf and compileEnv

- Tuple
- GetItem



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Initialize

Tetllen

We need to **initialize r15** with the **start position** of the heap

lez

• passed in as rdi by the run-time.

e,

How shall we get a hold of this position?

To do so, our_code starts off with a prelude



Find the gap add the gap as pad
 2 zero out last bits

QUIZ

Is r15 8-byte aligned?

A. Yes

B. No 🔨



1. Copy the value off the (parameter) stack, and

2. Adjust the value to ensure the value is 8-byte aligned.

mov r15, rdi add r15, 8 and r15, 0x 111.... 000 61-bits

QUIZ

Why add 8 to r15? What would happen if we removed that operation?



Construct

To construct a pair (v1, v2) we directly implement the above strategy (07-eggeater.md/#2-construction): where n=length vs compileEnv env (Tuple v1 v2) tupleAlloc (n+1) -- 1. allocate pair, resulting a = pairAlloc ddr in `rax` ++ sairCopy First (immArg env v1) -- 2. copy first value into slot ++ pairCopy Second (immArg env v2) -- 3. copy second value into slo 1 t -- 3. set the tag-bits of `rax` ++ setTag RAX TPair Lets look at each step in turn. APAX, 1 pairCopy fild arg = pair Alloc = mov rax, r15 mov rbx, arg mov [rax+of], rbx [rax+off] add r15, 16 where = field off fld tuple Alloc K = lrbp + mor rax, ris add ris, 8.K

Allocate

ris

To allocate, we just copy the current pointer **r15** and increment by **16** bytes,

• accounting for two 8-byte blocks for each element.

```
pairAlloc :: Asm
pairAlloc
= [ IMov (Reg RAX) (Reg R15) -- copy current "free address" `esi
` into `eax`
, IAdd (Reg RAX) (Const 16) -- increment `esi` by 8
]
```

Exercise How would you make this work for n -tuples?

We copy an Arg into a Field by

- saving the Arg into a helper register rbx,
- copying rbx into the field's slot on the heap.



Kes

Recall, the field's slot is either [rax] or [rax + 8] depending on whether the field is First or Second.

SRBP -

QUIZ

What shall we fill in for <u>1</u> and <u>2</u>?



[RBP-3*i]

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C. 1 and 2

D. -1 and -2

E. huh?

Tag

Finally, we set the tag bits of rax by using typeTag TPair which is defined

```
setTag :: Register -> Asm
setTag r = [ IAdd (Reg r) (HexConst 0x1) ]
```



we remove the tag bits by doing the opposite of setTag namely:

```
unsetTag :: Register -> Asm
unsetTag r = ISub (Reg RAX) (HexConst 0x1)
```

N-ary Tuples

Thats it! Lets take our compiler out for a spin, by using it to write some interesting programs!

First, lets see how to generalize pairs to allow for

- triples (e1,e2,e3)
- quadruples (e1,e2,e3,e4)
- pentuples (e1,e2,e3,e4,e5)

and so on.

 $(e_1, (e_2, e_3))$

 $(e_1, (e_2, (e_3, (e_4, -))))$

We just need a library of functions in our new egg language to

- Construct such tuples, and
- Access their fields.

Constructing Tuples

We can write a small set of functions to **construct** tuples (up to some given size):



Accessing Tuples

We can write a single function to access tuples of any size.

So the below code

```
let yuple = (10, (20, (30, (40, (50, false))))) in
```

get(yuple, 0) = 10
get(yuple, 1) = 20
get(yuple, 2) = 30
get(yuple, 3) = 40
get(yuple, 4) = 50

def tup3(x1, x2, x3):
 (x1, (x2, x3))

```
def tup5(x1, x2, x3, x4, x5):
   (x1, (x2, (x3, (x4, x5))))
```

```
let t = tup5(1, 2, 3, 4, 5) in
, x0 = print(get(t, 0))
, x1 = print(get(t, 1))
, x2 = print(get(t, 2))
, x3 = print(get(t, 3))
, x4 = print(get(t, 4))
in
```

99

should print out:

How shall we write it?

def get(t, i):
 TODO-IN-CLASS

QUIZ

Using the above "library" we can write code like:

```
let quad = tup4(1, 2, 3, 4) in
get(quad, 0) + get(quad, 1) + get(quad, 2) + get(quad, 3)
```

What will be the result of compiling the above?

Compile error
 Segmentation fault
 Other run-time error
 4
 4
 5. 10

QUIZ

Using the above "library" we can write code like:

```
def get(t, i):
    if i == 0:
        t[0]
    else:
        get(t[1],i-1)

def tup3(x1, x2, x3):
    (x1, (x2, (x3, false)))

let quad = tup3(1, 2, 3) in
    get(quad, 0) + get(quad, 1) + get(quad, 2) + get(quad, 3)
```

What will be the result of compiling the above?

- 1. Compile error
- 2. Segmentation fault
- 3. Other run-time error
- 4. 4
- 5. 10

Lists

Once we have pairs, we can start encoding **unbounded lists**.

To build a list, we need two constructor functions:

```
def empty():
   false
def cons(h, t):
   (h, t)
...
```

We can now encode lists as:

```python
cons(1, cons(2, cons(3, cons(4, empty()))))

#### Access

To access a list, we need to know

1. Whether the list is Empty, and

2. A way to access the head and the tail of a non-empty list.

```
def isEmpty(l):
 l == empty()

def head(l):
 l[0]

def tail(l):
 l[1]
```

#### Examples

We can now write various functions that build and operate on lists, for example, a function to generate the list of numbers between i and j

```
def range(i, j):
 if (i < j):
 cons(i, range(i+1, j))
 else:
 empty()</pre>
```

range(1, 5)

which should produce the result

(1,(2,(3,(4,false))))

and a function to sum up the elements of a list:

```
def sum(xs):
 if (isEmpty(xs)):
 0
 else:
 head(xs) + sum(tail(xs))
sum(range(1, 5))
```

which should produce the result 10.

### Recap

We have a pretty serious language now, with:

• Data Structures

which are implemented using

- Heap Allocation
- Run-time Tags

which required a bunch of small but subtle changes in the

• runtime and compiler

In your assignment, you will add *native* support for n-ary tuples, letting the programmer write code like:

e1[e2] *# allowing expressions to be used as fields* 

Next, we'll see how to

- use the "tuple" mechanism to implement higher-order functions and
- reclaim unused memory via garbage collection.

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