× 26 Functions

RSP/RBP

Next, we'll build diamondback which adds support for

• User-Defined Functions

In the process of doing so, we will learn about

- Static Checking
- Calling Conventions

G What TR? How Loop

Tail Recursion

X86-64

Plan

1. Defining Functions

2. Checking Functions

3. Compiling Functions

4. Compiling Tail Calls Only "loop"

1. Defining Functions

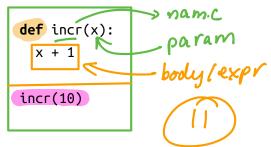
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First, lets add functions to our language.

As always, lets look at some examples.

Example: Increment

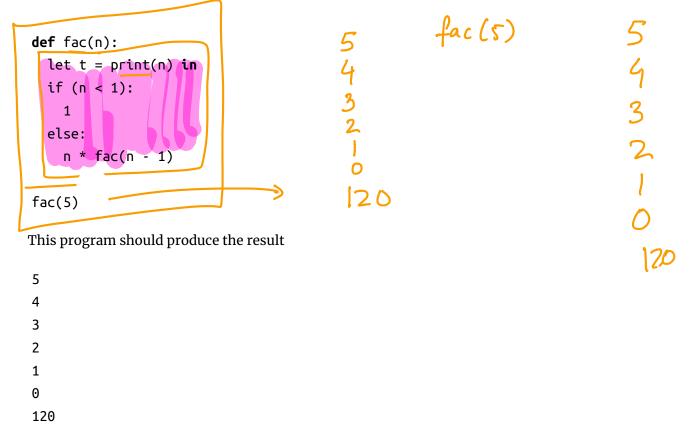
For example, a function that increments its input:



We have a function definition followed by a single "main" expression, which is evaluated to yield the program's result 11.

Example: Factorial

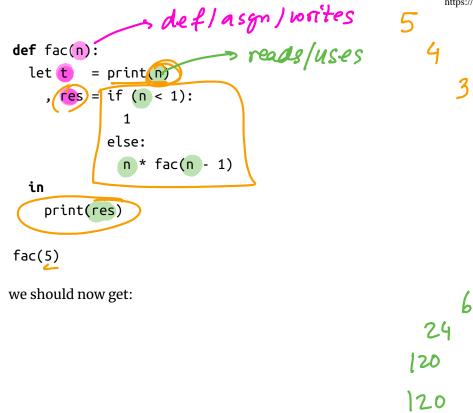
Here's a somewhat more interesting example:



Suppose we modify the above to produce intermediate results:

2

Z

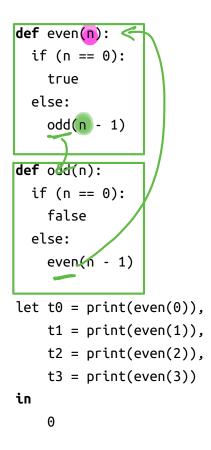


Example: Mutually Recursive Functions

For this language, the function definitions are global

any function can call any other function.

This lets us write *mutually recursive* functions like:



QUIZ What should be the result of executing the above?

false true false true 0
 true false true false 0
 false false false false 0

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4. true true true 0

Types

Lets add some new types to represent programs. Expra data Funca: Func Expra data Funca: Binda Formas: [Binda]

Binda = Bind Ida

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data Prog = Proj [Funca] (Expre)

Bindings

Lets create a special type that represents places where variables are bound,

data Bind a = Bind Id a

A Bind is an Id decorated with an a

- to save extra metadata like tags or source positions
- to make it easy to report errors.

We will use Bind at two places:

1. Let-bindings,

2. Function parameters.

It will be helpful to have a function to extract the Id corresponding to a Bind

cse131

bindId :: Bind a -> Id bindId (Bind x _) = x

Programs

A program is a list of declarations and main expression.

```
data Program a = Prog
{ pDecls :: [Decl a] -- ^ function declarations
, pBody :: !(Expr a) -- ^ "main" expression
}
```

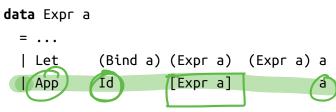
Declarations

Each function lives is its own declaration,

```
data Decl a = Decl
{ fName :: (Bind a) -- ^ name
, fArgs :: [Bind a] -- ^ parameters
, fBody :: (Expr a) -- ^ body expression
, fLabel :: a -- ^ metadata/tag
}
```

Expressions

Finally, lets add *function application* (calls) to the source expressions:



An application or call comprises

- an Id, the name of the function being called,
- a list of expressions corresponding to the parameters, and
- a metadata/tag value of type a.

(Note: that we are now using Bind instead of plain Id at a Let.)

Examples Revisited

Lets see how the examples above are represented:

incr fac

```
>>> parseFile "tests/input/incr.diamond"
Prog {pDecls = [Decl { fName = Bind "incr" ()
                     , fArgs = [Bind "n" ()]
                     , fBody = Prim2 Plus (Id "n" ()) (Number 1 ())
()
                     , fLabel = ()
               ]
     , pBody = App "incr" [Number 5 ()] ()
     }
>>> parseFile "tests/input/fac.diamond"
Prog { pDecls = [ Decl {fName = Bind "fac" ()
                , fArgs = [Bind "n" ()]
                , fBody = Let (Bind "t" ()) (Prim1 Print (Id "n" ())
())
                          (If (Prim2 Less (Id "n" ()) (Number 1 ())
())
                             (Number 1 ())
                             (Prim2 Times (Id "n" ())
                                (App "fac" [Prim2 Minus (Id "n" ())
(Number 1 ()) ()] ())
                                ()) ()) ()
                , fLabel = ()}
```

2. Static Checking

.

Next, we will look at an *increasingly important* aspect of compilation, **pointing out** bugs in the code at compile time

Called **Static Checking** because we do this *without* (i.e. *before*) compiling and running the code.

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There is a huge spectrum of checks possible:

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- Code Linting jslint (http://jshint.com/), hlint (https://hackage.haskell.org /package/hlint)
- Static Typing

• Static Analysis

- Contract Checking
- Dependent or Refinement Typing (https://ucsd-progsys.github.io/liquidhaskellblog/)

Increasingly, *this* is the most important phase of a compiler, and modern compiler engineering is built around making these checks lightning fast. For more, see this interview of Anders Hejlsberg (https://www.infoq.com/news/2016/05/andershejlsberg-compiler) the architect of the C# and TypeScript compilers.

Language SERVERS

Static Well-formedness Checking

We will look at code linting and, later in the quarter, type systems in 131.

For the former, suppose you tried to compile:

```
def fac(n):
    let t = print(n) in
    if (n < 1):
        1
    else:
        n * fac(m - 1)
fact(5) + fac(3, 4)</pre>
```

We would like compilation to fail, not silently, but with useful messages:

```
$ make tests/output/err-fac.result
```

Errors found!

tests/input/err-fac.diamond:6:13-14: Unbound variable 'm'

```
6| n * fac(m - 1)
```

tests/input/err-fac.diamond:8:1-9: Function 'fact' is not defined

8| fact(5) + fac(3, 4)

tests/input/err-fac.diamond:(8:11)-(9:1): Wrong arity of arguments at call of fac

8| fact(5) + fac(3, 4)

We get *multiple* errors:

1. The variable m is not defined,

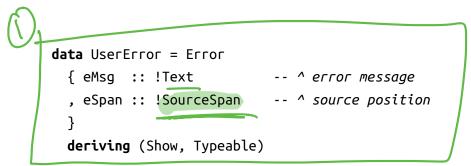
2. The function fact is not defined,

3. The call fac has the wrong number of arguments.

Next, lets see how to update the architecture of our compiler to support these and other kinds of errors.

Types: An Error Reporting API

An error message type:



We make it an *exception* (that can be *thrown*):

```
() instance Exception [UserError]
```

We can **create** errors with:

```
mkError :: Text -> SourceSpan -> Error
mkError msg l = Error msg l
```

We can **throw** errors with:

```
abort :: UserError -> a
abort e = throw [e]
```

We display errors with:

```
renderErrors :: [UserError] -> IO Text
```

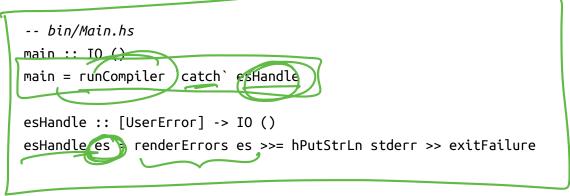
which takes something like:

```
Error
"Unbound variable 'm'"
{ file = "tests/input/err-fac"
, startLine = 8
, startCol = 1
, endLine = 8
, endCol = 9
}
```

and produces a contextual message (that requires reading the source file),

```
tests/input/err-fac.diamond:6:13-14: Unbound variable 'm'
```

We can put it all together by



Which runs the compiler and if any UserError are thrown, catch -es and renders the result.

Transforms

Next, lets insert a checker phase into our pipeline:

Compiler Pipeline with Checking Phase

In the above, we have defined the types:

```
type BareP = Program SourceSpan -- ^ source position metadat
a
type AnfP = Program SourceSpan -- ^ sub-exprs in ANF
type AnfTagP = Program (SourceSpan, Tag) -- ^ sub-exprs have unique t
ag
```

Catching Multiple Errors

Its rather irritating to get errors one-by-one.

To make using a language and compiler pleasant, lets return *as many errors as possible* in each run.

We will implement this by writing the functions

```
wellFormed :: BareProgram -> [UserError]
```

which will *recursively traverse* the entire program, declaration and expression and return the *list of all errors*.

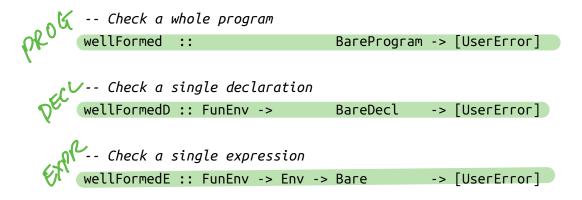
- If this list is empty, we just return the source unchanged,
- Otherwise, we throw the list of found errors (and exit.)

Thus, our check function looks like this:

```
check :: BareProgram -> BareProgram
check p = case wellFormed p of
    [] -> p
    es -> throw es
```

Well-formed Programs, Declarations and Expressions

The bulk of the work is done by three functions



Well-formed Programs

To check the whole program

This function,

- 1. **Creates** FunEnv, a map from *function-names* to the *function-arity* (number of params),
- 2. Computes the errors for each declaration (given functions in fEnv),
- 3. Concatenates the resulting lists of errors.

Which function(s) would we have to modify to add *large number errors* (i.e. errors for numeric literals that may cause overflow)?

```
    wellFormed :: BareProgram -> [UserError]
    wellFormedD :: FunEnv -> BareDecl -> [UserError]
    wellFormedE :: FunEnv -> Env -> Bare -> [UserError]
    1 and 2
    2 and 3
```

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let = 10,x = 20

Which function(s) would we have to modify to add variable shadowing errors ?

| | | d | P |
|----|--|--------|------|
| | 1. wellFormed :: BareProgram -> [UserError] | Lay | Func |
| ? | 2. wellFormedD :: FunEnv -> BareDecl -> [UserError] | ÷ | |
| 2 | 3. wellFormedE :: FunEnv -> Env -> Bare -> [UserErro | or] | |
| ્વ | 4. 1 and 2 | - | |
| | 5. 2 and 3 | N. | (|
| | | Ano Ve | 51 |
| | | Kup | |

Which function(s) would we have to modify to add duplicate parameter errors?

```
1. wellFormed :: BareProgram -> [UserError]
2. wellFormedD :: FunEnv -> BareDecl -> [UserError]
3. wellFormedE :: FunEnv -> Env -> Bare -> [UserError]
4. 1 and 2
5. 2 and 3
```

Which function(s) would we have to modify to add duplicate function errors?

1. wellFormed :: BareProgram -> [UserError] 2. wellFormedD :: FunEnv -> BareDecl -> [UserError] 3. wellFormedE :: FunEnv -> Env -> Bare -> [UserError] 4. 1 and 2 5. 2 and 3) iamond Checking Compile fun<u>lcalls</u> Tail Calls

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Traversals

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arity



Lets look at how we might check for two types of errors:

1. "unbound variables" 2. "undefined functions"



(In your assignment, you will look for **many** more.)

The helper function wellFormedD creates an *initial* variable environment vEnv containing the functions parameters, and uses that (and fEnv) to walk over the body-expressions.

```
wellFormedD :: FunEnv -> BareDecl -> [UserError]
wellFormedD fEnv (Decl _ xs e _) = wellFormedE fEnv vEnv e
where
vEnv = addsEnv xs emptyEnv
```

The helper function wellFormedE starts with the input

- vEnv0 which has the function parameters, and
- fEnv that has the defined functions,

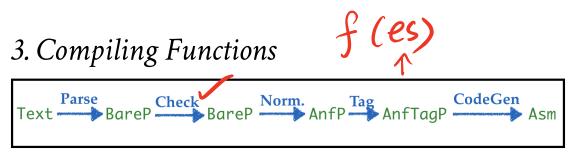
and traverses the expression:

- At each **definition** Let x e1 e2, the variable x is added to the environment used to check e2,
- At each use Id x we check if x is in vEnv and if not, create a suitable UserError

• At each call App f es we check if f is in fEnv and if not, create a suitable UserError.

```
wellFormedE :: FunEnv -> Env -> Bare -> [UserError]
wellFormedE fEnv vEnv0 e  = go vEnv0 e
where
gos vEnv es = concatMap (go vEnv) es
go _ (Boolean {}) = []
go _ (Number n l) = []
go vEnv (Id x l) = unboundVarErrors vEnv x l
go vEnv (Prim1 _ e _) = go vEnv e
go vEnv (Prim2 _ e1 e2 _) = gos vEnv [e1, e2]
go vEnv (If e1 e2 e3 _) = gos vEnv [e1, e2, e3]
go vEnv (Let x e1 e2 _) = go vEnv e1
++ go (addEnv x vEnv) e2
go vEnv (App f es l) = unboundFunErrors fEnv f l
++ gos vEnv es
```

You should understand the above and be able to easily add extra error checks.



Compiler Pipeline for Functions

In the above, we have defined the types:

```
type BareP = Program SourceSpan -- ^ each sub-expression has
source position metadata
type AnfP = Program SourceSpan -- ^ each function body in A
NF
type AnfTagP = Program (SourceSpan, Tag) -- ^ each sub-expression has
unique tag
```

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Text BareP Check BareP AnfP AnfTagP CodeGen Asm

Compiler Pipeline ANF

The tag phase simply recursively tags each function body and the main expression

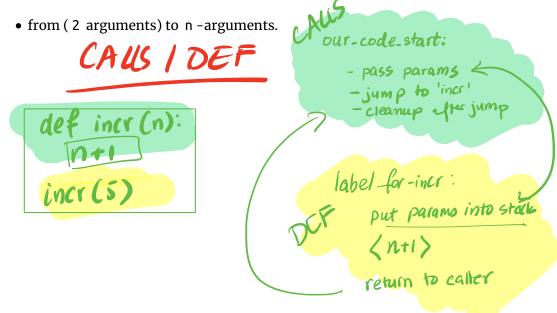
ANF Conversion



Compiler Pipeline ANF

- The normalize phase (i.e. anf) is recursively applied to each function body.
- In addition to Prim2 operands, each call's arguments should be transformed into an immediate expression (04-boa.md/#idea-immediate-expressions)

Generalize the strategy for *binary* operators (04-boa.md/#anf-implementation)



Strategy

Now, lets look at compiling function definitions and calls.



Compiler Pipeline with Checking Phase

We need a co-ordinated strategy for *definitions* and *calls*.

unction Definitions

- Each *definition* is compiled into a labeled block of Asm
- That implements the *body* of the definitions.
- (But what about the parameters)?

Function Calls

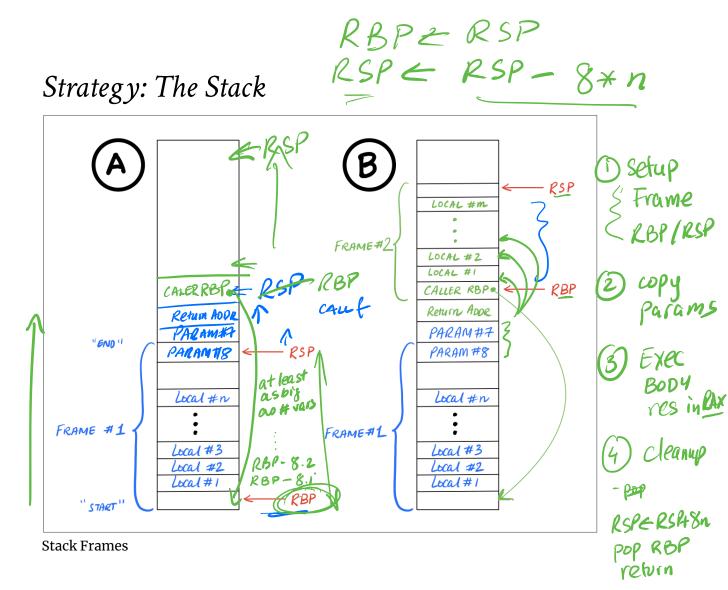
 d_1 d_2

az

• Each call of f(args) will execute the block labeled f

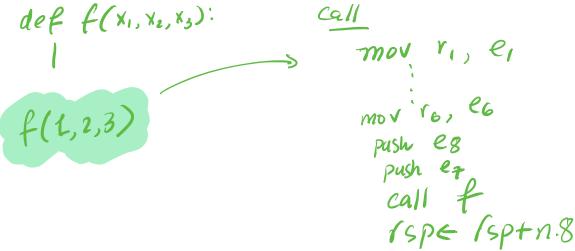
• (But what about the parameters)?

(e) (d_i) (d_2) (d_3)



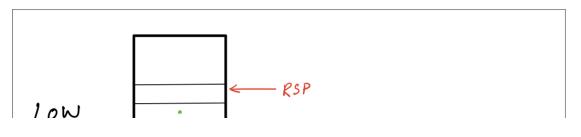
We will use our old friend, the stack to

- pass parameters
- have local variables for called functions.



X86-64 Calling Convention

We are using the x86-64 calling convention (https://aaronbloomfield.github.io /pdr/book/x86-64bit-ccc-chapter.pdf), that ensures the following stack layout:



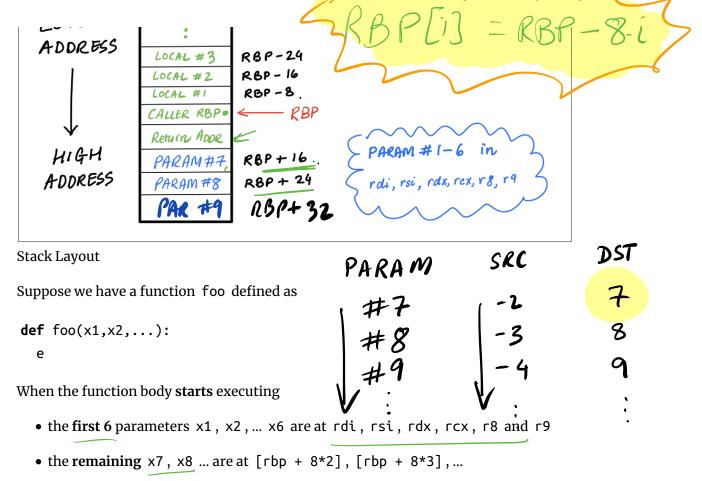
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https://ucsd-cse131.github.io/sp21/lectures/06-diamond.html



```
When the function exits
```

• the **return** value is in rax

Pesky detail on Stack Alignment

At both *definition* and *call*, you need to also respect the 16-Byte Stack Alignment Invariant (https://en.wikipedia.org/wiki/X86_calling_conventions)

Ensure rsp is always a multiple of 16.

i.e. pad to ensure an even number of arguments on stack

dof incln): n+1 (main) (di) <02 incls.



Strategy: Definitions

Calls.

Thus to compile each definition

def foo(x1,x2,...):
 body

we must

- part 1 cop
- 1. **Setup Frame** to *allocate* space for local variables by ensuring that rsp and rbp are properly managed (.../lectures/05-cobra.md/#managing-the-call-stack)
- 2. **Copy parameters** x1, x2, ... from the registers & stack into stack-slots 1, 2, ... so we can access them in the body

3. Compile Body body with initial Env mapping parameters $x1 \Rightarrow 1, x2 \Rightarrow 2,$

4. Teardown Frame to restore the caller's rbp and rsp prior to ret urn.

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Strategy: Calls

As before (../lectures/05-cobra.md/#in-the-caller) we must ensure that the parameters actually live at the above address.

1. Push the parameter values into the registers & stack,

2. Call the appropriate function (using its label),

3. Pop the arguments off the stack by incrementing rsp appropriately. *Add(x,y): x+Y x*

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def add 10(x1;...,x10): X1+X2+...+X10 add 10 (1,2,3,...,10) dof-fun-addid: Types We already have most of the machinery needed to compile calls. Lets just add a new kind of Label for each user-defined function: data Label = ...

| DefFun Id

Implementation

Lets can refactor our compile functions into:

-- Compile the whole program compileProg :: AnfTagP -> Asm

-- Compile a single function declaration compileDecl :: Bind -> [Bind] -> Expr -> Asm

-- Compile a single expression compileExpr :: Env -> AnfTagE -> Asm

that respectively compile Program, Decl and Expr.

Compiling Programs

To compile a Program we compile

- the main expression as Decl with no parameters and
- each *function* declaration

```
compileProg (Prog ds e) =
    compileDecl (Bind "" ()) [] e
++ concat [ compileDecl f xs e | (Decl f xs e _) <- ds ]</pre>
```

QUIZ

Does it matter whether we put the code for e before ds?

1. Yes

2. No

QUIZ

Does it matter what order we compile the ds $\ ?$

1. Yes

2. No

Compiling Declarations

To compile a single ${\tt Decl}$ we

- 1. Create a block starting with a label for the function's name (so we know where to call),
- 2. Invoke compileBody to fill in the assembly code for the body, using the initial Env obtained from the function's formal parameters.

```
compileDecl :: Bind a -> [Bind a] -> AExp -> [Instruction]
compileDecl f xs body =
 -- 0. Label for start of function
    [ ILabel (DefFun (bindId f)) ]
 -- 1. Setup stack frame RBP/RSP
 ++ funEntry n
 -- label the 'body' for tail-calls
 ++ [ ILabel (DefFunBody (bindId f)) ]
 -- 2. Copy parameters into stack slots
 ++ copyArgs xs
 -- 3. Execute 'body' with result in RAX
 ++ compileEnv initEnv body
 -- 4. Teardown stack frame & return
 ++ funExit n
 where
            = countVars body
    n
    initEnv = paramsEnv xs
```

Setup and Tear Down Stack Frame

(As in cobra) $% \left(As \left({{{\left({As} \right)}_{n}}} \right)$

Setup frame

```
funEntry :: Int -> [Instruction]
funEntry n =
  [ IPush (Reg RBP) -- save caller's RBP
  , IMov (Reg RBP) (Reg RSP) -- set callee's RBP
  , ISub (Reg RSP) (Const (argBytes n)) -- allocate n local-vars
  ]
```

Teardown frame

```
funExit :: Int -> [Instruction]
funExit n =
   [ IAdd (Reg RSP) (Const (argBytes n)) -- un-allocate n local-va
rs
  , IPop (Reg RBP) -- restore callee's RBP
  , IRet -- return to caller
]
```

Copy Parameters into Frame

copyArgs xs returns the instructions needed to copy the parameter values

- From the combination of rdi, rsi, ...
- To this function's frame, rdi -> [rbp 8], rsi -> [rbp 16],...

```
copyArgs :: [a] -> Asm
copyArgs xs
             = copyRegArgs rXs -- copy upto 6 register args
             ++ copyStackArgs sXs -- copy remaining stack args
 where
    (rXs, sXs) = splitAt 6 xs
-- Copy upto 6 args from registers into offsets 1..
copyRegArgs :: [a] -> Asm
copyRegArgs xs = [ IMov (stackVar i) (Reg r) | ( ,r,i) <- zipWith3 xs
regs [1..] ]
 where regs = [RDI, RSI, RDX, RCX, R8, R9]
-- Copy remaining args from stack into offsets 7..
copyStackArgs :: [a] -> Asm
copyStackArgs xs = concat [ copyArg src dst | ( ,src,dst) <- zip3 xs
[-2,-3..] [7..]]
-- Copy from RBP-offset-src to RBP-offset-dst
copyArg :: Int -> Int -> Asm
copyArg src dst =
  [ IMov (Reg RAX) (stackVar src)
  , IMov (stackVar dst) (Reg RAX)
```

Execute Function Body

(As in cobra)

compileEnv initEnv body generates the assembly for e using initEnv, the initial Env created by paramsEnv

paramsEnv :: [Bind a] -> Env
paramsEnv xs = fromListEnv (zip xids [1..])
where
xids = map bindId xs

paramsEnv xs returns an Env mapping each parameter to its stack position

(Recall that bindId extracts the Id from each Bind)

Compiling Calls

Finally, lets extend code generation to account for calls:

```
compileEnv :: Env -> AnfTagE -> [Instruction]
compileEnv env (App f vs _) = call (DefFun f) [immArg env v | v <- v
s]</pre>
```

EXERCISE The hard work in compiling calls is done by:

```
call :: Label -> [Arg] -> [Instruction]
```

which implements the strategy for calls. Fill in the implementation of call yourself. As an example, of its behavior, consider the (source) program:

```
def add2(x, y):
    x + y
    add2(12, 7)
The call add2(12, 7) is represented as:
```

App "add2" [Number 12, Number 7]

The code for the above call is generated by

```
call (DefFun "add2") [arg 12, arg 7]
```

where arg converts source values into assembly Arg (../lectures/05-cobra.md/a-typeclass-for-representing-constants) which *should* generate the equivalent of the assembly:

```
mov rdi 24
mov rsi 14
call label_def_add2
```

4. Compiling Tail Calls

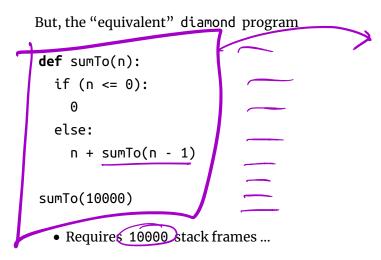
Our language doesn't have *loops*. While recursion is more general, it is more *expensive* because it uses up stack space (and requires all the attendant management overhead).

For example (the python program):

```
def sumTo(n):
    r = 0
    i = n
    while (0 <= i):
        r = r + i
        i = i - 1
    return r</pre>
```

sumTo(10000)

- Requires a *single* stack frame
- Can be implemented with 2 registers



• One for fac(10000), one for fac(9999) etc.

Tail Recursion

Fortunately, we can do much better.

A **tail recursive** function is one where the recursive call is the *last* operation done by the function, i.e. where the value returned by the function is the *same* as the value returned by the recursive call.

We can rewrite sumTo using a tail-recursive loop function:

```
def loop(r, i):
    if (0 <= i):
        let rr = r + i
        , ii = i - 1
        in
        loop(rr, ii)  # tail call
    else:
        r

def sumTo(n):
    loop(0, n)
sumTo(10000)</pre>
```

Visualizing Tail Calls

Lets compare the execution of the two versions of sumTo

Plain Recursion

$$sumTo(5) ==> 5 + sumTo(4)$$

$$==> 5 + [4 + sumTo(3)]$$

$$==> 5 + [4 + [3 + sumTo(2)]]$$

$$==> 5 + [4 + [3 + [2 + sumTo(1)]]]$$

$$==> 5 + [4 + [3 + [2 + [1 + sumTo(0)]]]]$$

$$==> 5 + [4 + [3 + [2 + [1 + 0]]]]$$

$$==> 5 + [4 + [3 + [2 + 1]]]$$

$$==> 5 + [4 + [3 + [2 + 1]]]$$

$$==> 5 + [4 + [3 + 3]]$$

$$==> 5 + [4 + 6]$$

$$==> 5 + 10$$

$$==> 15$$

• Each call **pushes a frame** onto the call-stack;

Tail Recursion

```
sumTo(5)
==> loop(0, 5)
==> loop(5, 4)
==> loop(9, 3)
==> loop(12, 2)
==> loop(14, 1)
==> loop(15, 0)
==> 15
```

- Accumulation happens in the parameter (not with the output),
- Each call returns its result without further computation

No need to use call-stack, can make recursive call **in place**. * Tail recursive calls can be *compiled into loops*!

Tail Recursion Strategy

Instead of using call to make the call, simply:

1. Copy the call's arguments to the (same) stack position (as current args),

- first six in rdi, rsi etc. and rest in [rbp+16], [rbp+18]...
- 2. Jump to the *start* of the function
- but *after* the bit where setup the stack frame (to not do it again!)

That is, here's what a naive implementation would look like:

```
mov rdi, [rbp - 8]  # push rr
mov rsi, [rbp - 16]  # push ii
call def_loop
```

but a *tail-recursive* call can instead be compiled as:

mov rdi, [rbp - 8] # push rr mov rsi, [rbp - 16] # push ii jmp def_loop_body

which has the effect of executing loop *literally* as if it were a while-loop!

How to KNOW if call is TR?
How to complete the TR all?
Add-label, replace call - jump

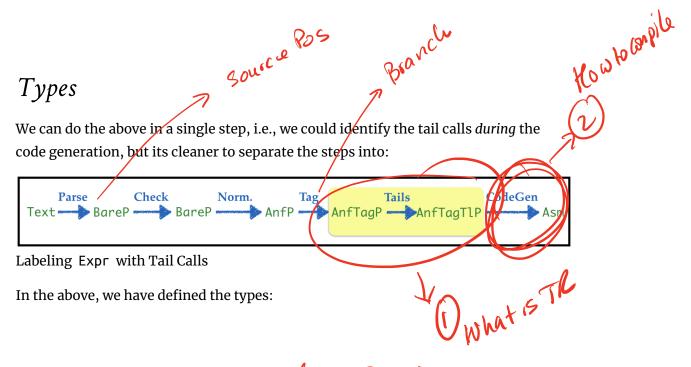
Requirements

To *implement* the above strategy, we need a way to:

1. Identify tail calls in the source Expr (AST),

2. Compile the tail calls following the above strategy.

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Prog a -> Proj (a, Bool)

```
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```

```
type BareP = Program SourceSpan -- ^ each sub-exp
ression has source position metadata
type AnfP = Program SourceSpan -- ^ each functio
n body in ANF
type AnfTagP = Program (SourceSpan, Tag) -- ^ each sub-exp
ression has unique tag
type AnfTagTLP = Program ((SourceSpan, Tag), Bool) -- ^ each call is
marked as "tail" or not
```

Transforms

Thus, to implement tail-call optimization, we need to write two transforms:

1. To Label each call with True (if it is a *tail call*) or False otherwise:

fool bar baz 4/27/21, 9:12 AM

tails :: Program a -> Program (a, Bool)

2. To Compile tail calls, by extending compileEnv

| Prog | 2 | [Decl] |
|------|---|--------------|
| Decl | 1 | ([1d], Expr) |

Expr = Number* 1 Id. 1 Prm1 Op Expr 1 Prim2 Op Expr 1 Let Id Expr Expr 1 If Expr Expr App Id [Expr] Labeling Tail Calls

10+f(1,2,3): not TR def f(x,q,z): Can we turn $g(y,z) \leftarrow this inbo$ $<math>g(y,z) \leftarrow a JUMP S$ (a) YES dog g(a,b): NO

| | data |
|---|------|
| <pre>def facTR(acc, n):</pre> | = N |
| if (n < 1): | IE |
| acc | |
| else: | |
| if (n == 2): | I P |
| 2 * facTR(n - 1, n - 1) Not Tail | I P |
| else: |] |
| facTR(acc * n, n - 1) Tail | 1 11 |
| ructulate i up u 27 full | |
| | |
| | |
| U les dia bin op plinte | |
| (1) rec (2) ainvolved in Lin op Primiz (2) ainvolved in Lin op Primiz Unavy Primiz | |

| dat | 20 | a Expr | | | |
|-----|----|---------|--------|--------|------|
| = | = | Number | Intege | er | |
| | | Boolean | Bool | | |
| | | Id | Id | | |
| | | Prim1 | Prim1 | Expr | |
| | | Prim2 | Prim2 | Expr | Expr |
| | | If | Expr | Expr | Expr |
| | | Let | Bind | Expr | Expr |
| | | Арр | Id | [Expr] | |



Which Calls are Tail Calls?

The Expr in non tail positions

- Prim1
- Prim2
- Let ("bound expression")
- If ("condition")

cannot contain tail calls; all those values have some further computation performed on them.

However, the Expr in tail positions

- If ("then" and "else" branch)
- Let ("body")

can contain tail calls (unless they appear under the first case)

Algorithm: Traverse Expr using a Bool

- Initially True but
- Toggled to False under non-tail positions,
- Used as "tail-label" at each call.

NOTE: All non-calls get a default tail-label of False.

```
tails :: Expr a -> Expr (a, Bool)
tails = go True
                                                    -- initially
flag is True
 where
   noTail l z
               = z (l, False)
   go _ (Number n l) = noTail l (Number n)
   go _ (Boolean b l) = noTail l (Boolean b)
   go_(Id xl)
                         = noTail l (Id x)
   go _ (Prim2 o e1 e2 l) = noTail l (Prim2 o e1' e2')
     where
       [e1', e2'] = go False <$> [e1, e2] -- "prim-arg
s" is non-tail
   go b (If c e1 e2 l) = noTail l (If c' e1' e2')
     where
       c'
                         = go False c
                                                    -- "cond" is
non-tail
       e1'
                                                    -- "then" may
                         = qo b
                                   e1
be tail
                                                   -- "else" may
       e2'
                         = go b
                                   e2
be tail
```

go b (Let x e1 e2 l) = noTail l (Let x e1' e2')

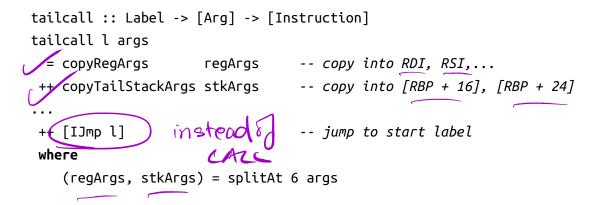
| where | | |
|-------------------|--------------------|----------------|
| e1' | = go False e1 | "bound-exp |
| r" is non-tail | | |
| e2' | = go b e2 | "body-exp |
| r" may be tail | | |
| | | |
| go b (App f es l) | = App f es' (l, b) | tail-label |
| is current flag | | |
| where | | |
| es' | = go False <\$> es | "call arg |
| s" are non-tail | | |

EXERCISE: How could we modify the above to *only* mark **tail-recursive** calls, i.e. to the *same* function (whose declaration is being compiled?)

Compiling Tail Calls

Finally, to generate code, we need only add a special case to compileExpr

That is, *if* the call is *not labeled* as a tail call, generate code as before. Otherwise, use tailcall which implements our tail recursion strategy



Recap

We just saw how to add support for first-class function

- Definitions, and
- Calls 🧹

and a way in which an important class of

• Tail Recursive functions can be compiled as loops.

Later, we'll see how to represent **functions as values** using **closures**.

(https://ucsd-cse131.github.io/sp21/feed.xml)

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(https://github.com/ucsd-cse131/sp21)

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